

That's Not How I Learned It!

Multiplication & Division



Deep Run Elementary

Outcomes

By the end of the sessions, participants will have:

- Viewed and discussed the progression of multiplication
- Explored various strategies for multi-digit multiplication and division
- Received Write and Wipe Board w/ open array and open number lines for home use

Mental Math and Fluency Expectations

GRADE	END-OF-YEAR EXPECTATION	EXAMPLES
K	fluently + and – within 5	$4 + 1$ $5 - 2$ $3 + 2$
1	fluently + and – within 10	$7 - 5$ $4 + 3$ $9 - 6$
	± 10 for any two-digit number	$26 + 10$ $84 - 10$
2	know from memory all sums of two one-digit addends	$6 + 7$ $8 + 3$ $7 + 8$ $2 + 7$ $9 + 5$ $4 + 9$
	± 10 and ± 100 for any three-digit number	$473 - 10$ $816 + 10$ $352 - 100$ $709 + 100$
3	know from memory all products of one-digit factors	4×9 8×6 5×7 7×3 2×9 4×8

Computation Expectations by Grade

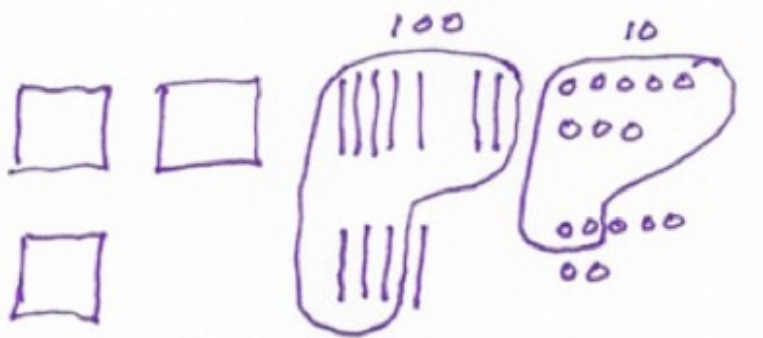
GRADE	END-OF-YEAR EXPECTATION
K	<ul style="list-style-type: none">• add and subtract within 10
1	<ul style="list-style-type: none">• add and subtract within 20• add within 100• subtract two-digit multiples of 10
2	<ul style="list-style-type: none">• add and subtract within 1,000
3	<ul style="list-style-type: none">• add and subtract within 1,000• multiply two one-digit factors• multiply one-digit factors by a multiple of 10
4	<ul style="list-style-type: none">• add and subtract within 1,000,000• multiply: 1 by 4 and 2 by 2• divide: up 4 by 1
5	<ul style="list-style-type: none">• multiply multi-digit numbers• divide: up to 4 by 2• perform all operations on decimals

Formal Algorithm Expectations by Grade

GRADE	END-OF-YEAR EXPECTATION
K	
1	
2	
3	

Formal Algorithm Expectations by Grade

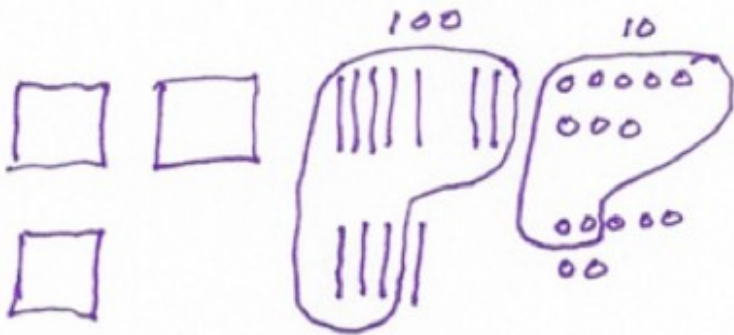
GRADE	END-OF-YEAR EXPECTATION
K	pictorial & concrete models



pictorial

Formal Algorithm Expectations by Grade

GRADE	END-OF-YEAR EXPECTATION
K	pictorial & concrete models
1	pictorial & concrete models ; written methods



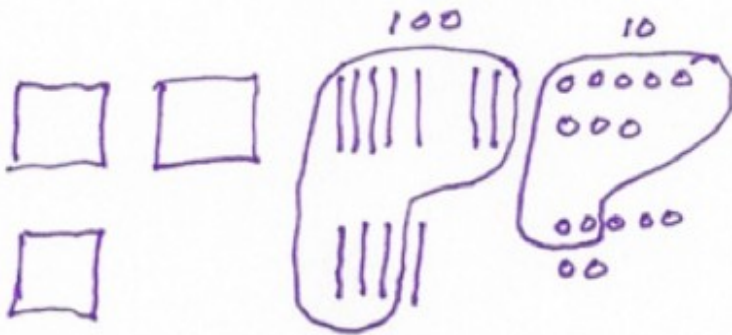
pictorial model

$$\begin{array}{r} 278 \\ +147 \\ \hline 300 \end{array} \quad \begin{array}{r} 278 \\ +147 \\ \hline 300 \\ 110 \end{array} \quad \begin{array}{r} 278 \\ +147 \\ \hline 300 \\ 110 \\ 15 \\ \hline 425 \end{array}$$

written method

Formal Algorithm Expectations by Grade

GRADE	END-OF-YEAR EXPECTATION
K	pictorial & concrete models
1	pictorial & concrete models ; written methods
2	pictorial & concrete models; written methods



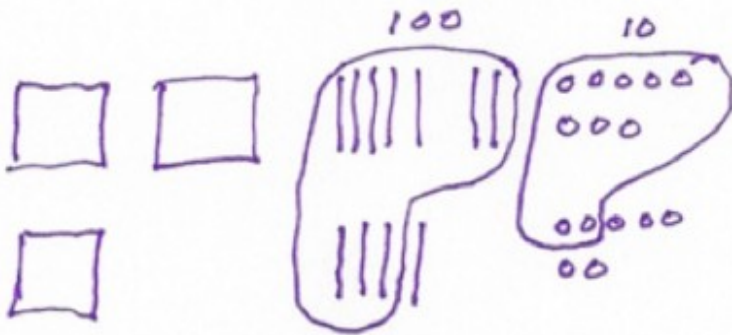
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pictorial model

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written method

Formal Algorithm Expectations by Grade

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K	pictorial & concrete models
1	pictorial & concrete models ; written methods
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3	pictorial & concrete models; written methods
4	whole number addition & subtraction (algorithm)
5	whole number multiplication (algorithm)
6	whole number division decimal computation: all operations

Formal Algorithm Expectations by Grade

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Formal Algorithm Expectations by Grade

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K	
1	
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4	whole number addition & subtraction (algorithm)
5	whole number multiplication (algorithm)
6	whole number division decimal computation: all operations

The Progression of Multiplication

Making Sense Series

the progression of multiplication
and
the standard traditional algorithm

created by Graham Fletcher



@gfletchy

00:06



-05:54

Building Proficiency

Modeling

base ten blocks



Building Proficiency

Modeling

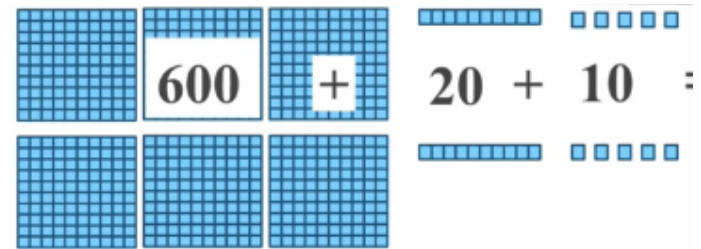
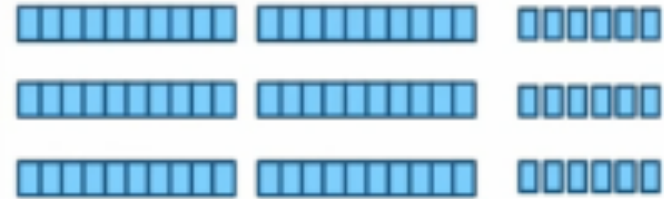
$$852 \div 4$$

$$\begin{array}{r}
 852 \\
 -400 \quad (\times 100) \\
 \hline
 452 \\
 -400 \quad (\times 100) \\
 \hline
 52 \\
 -40 \quad (\times 10) \\
 \hline
 12 \\
 -4 \quad (\times 1) \\
 \hline
 8 \\
 -4 \quad (\times 1) \\
 \hline
 4 \\
 -4 \quad (\times 1) \\
 \hline
 0
 \end{array}$$

base ten blocks
array models

area models

partial product
& partial quotient
models



	200	30	7
8	1600	240	56

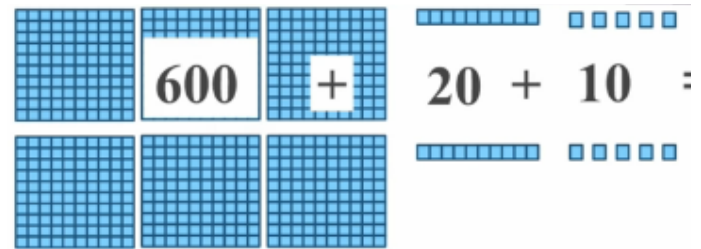
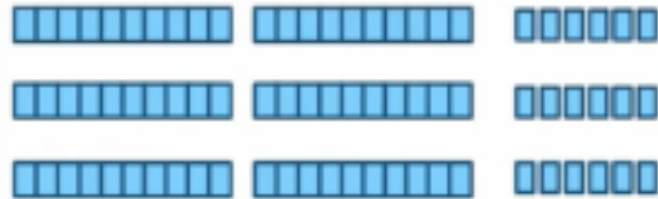
$$\begin{array}{r}
 45 \quad (40 + 5) \\
 \times 15 \quad (10 + 5) \\
 \hline
 25 \quad (5 \times 5) \\
 200 \quad (5 \times 40) \\
 50 \quad (10 \times 5) \\
 + 400 \quad (10 \times 40) \\
 \hline
 675
 \end{array}$$

Building Proficiency

Modeling

base ten blocks
array models

area models



	200	30	7
8	1600	240	56

Building Both Sides of the Brain

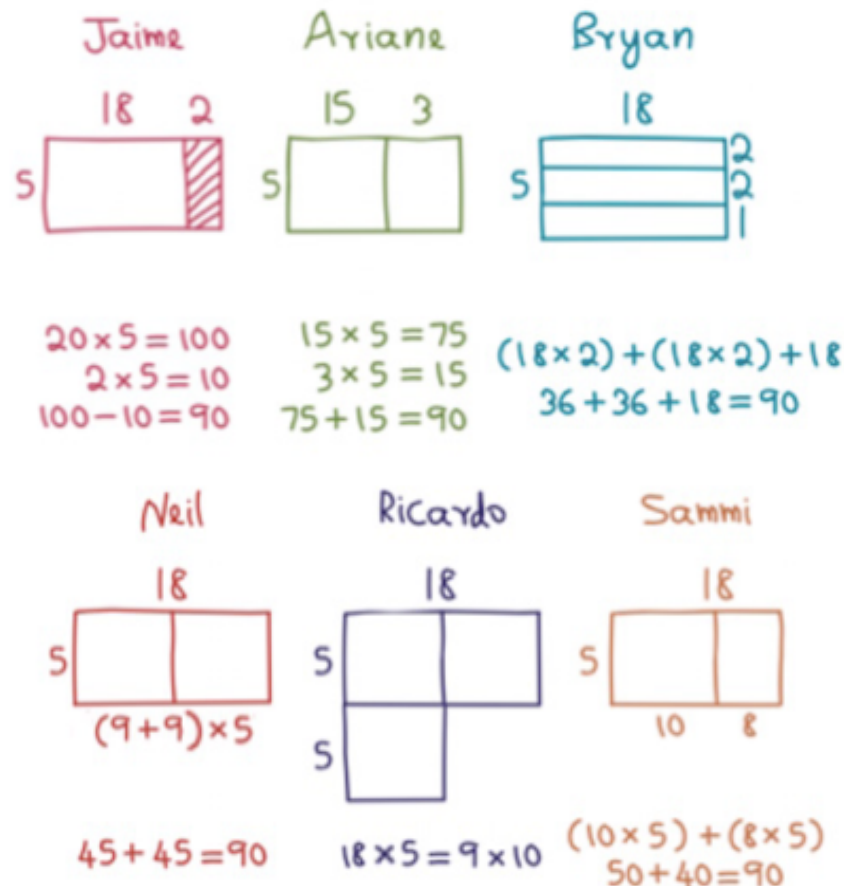
visual and spatial
information

+

symbolic
information



improved
mathematics
performance



Building Proficiency

Modeling

base ten blocks
array models

area models

partial product
& partial quotient
models

Decomposition

Building Proficiency

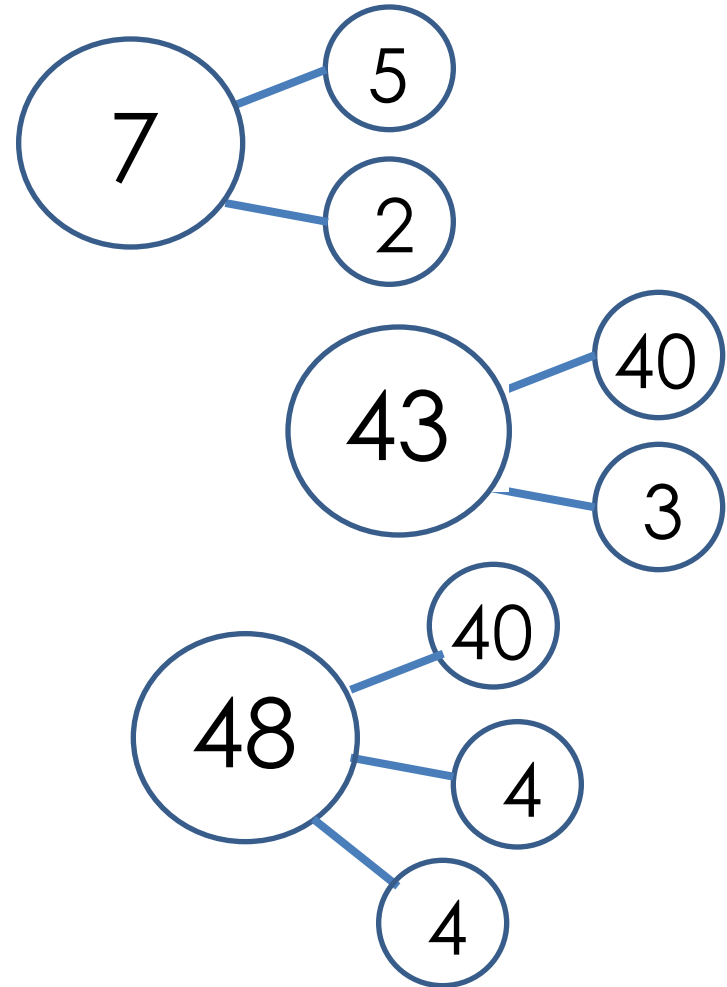
Modeling

base ten blocks
array models

area models

partial product
& partial quotient
models

Decomposition



Building Proficiency

Modeling

Decomposition

base ten blocks
array models

$$371 \rightarrow 300 \text{ \& } 70 \text{ \& } 1$$

area models

$$371 \rightarrow 300 \text{ \& } 60 \text{ \& } 11$$

partial product
& partial quotient
models

$$371 \rightarrow 350 \text{ \& } 21$$

$$371 \rightarrow 300 \text{ \& } 50 \text{ \& } 21$$

$$371 \rightarrow 360 \text{ \& } 11$$

Building Proficiency

Modeling

base ten blocks
array models

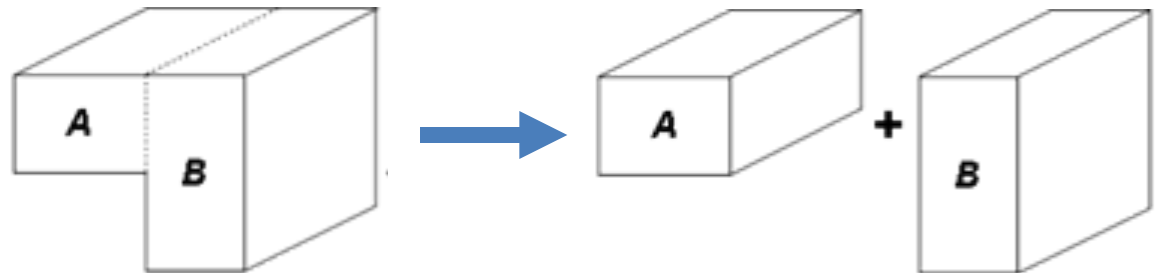
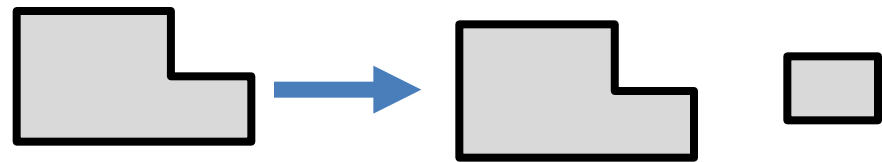
area models

partial product
& partial quotient
models

Decomposition

$$\frac{3}{4} \longrightarrow \frac{1}{4} \text{ \& } \frac{1}{4} \text{ \& } \frac{1}{4}$$

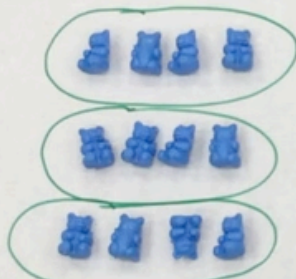
$$4.96 \longrightarrow 4 \text{ \& } 0.96$$



Progression of Division

The Progression
of Division

3rd grade $12 \div 4$



12 bears
4 in each group
measurement
OR
repeated subtraction
GROUPS?

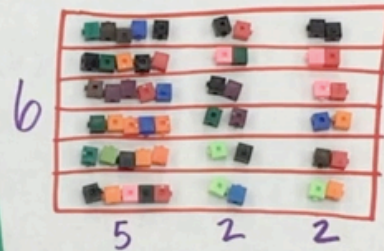


12 bears
shared with
4 friends
fair share
OR
partitioning
SIZE?

$54 \div 6$

000
000

efficient thinkers



	5	2	2	
6	30	12	12	
	$30 + 12 + 12 = 54$			

54
<u>-30</u> (6x5)
24
<u>12</u> (6x2)
12
<u>12</u> (6x2)
0

Progression of Division

Quotients > 10
 $72 \div 3$

↓

3	10	10	4
	30	30	12

3	20	4
	60	12

$72 = (3 \times 20) + (3 \times 4)$
 Distributive Property
 # Visually

4th grade 4 digit dividends ÷ 1 digit divisors

models representation written expression

$144 \div 9$

and so on....

EFFICIENT THINKING??

2

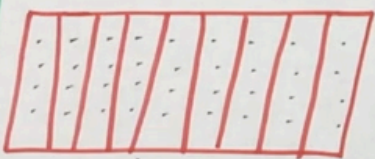
144
- 9
135
- 9
126
- 9
117
- 9
108
- 9
99
- 9
90
- 9
81
- 9
72
- 9
63
- 9
54
- 9
45
- 9
36
- 9
27
- 9
18
- 9
9
- 9
0

Progression of Division

4th grade 4 digit dividends ÷ 1 digit divisors

models representation ← written expression

$144 \div 9$



and so on....

EFFICIENT THINKING??

Area model for partial quotients

$3672 \div 9$

3672
 -9 1 group
 3663
 -9 1 group
 3654
 900 100 groups
 2754
 -1800 200 groups
 954
 900 100 groups
 54
 54 6 groups
 0

3672
 -1800
 1872
 -1800
 72
 -72
 0

200 200 8

9 1800 1800 72

144
 -9
 135
 -9
 126
 -9
 117
 -9
 108
 -9
 99
 -9
 90
 -9
 81
 -9
 72
 -9
 63
 -9
 54
 -9
 45
 -9
 36
 -9
 27
 -9
 18
 -9
 9
 -9
 0

Working Together to Build Mathematical Thinkers

The school's role...

- offer rich, purposeful mathematical experiences
- provide number strategy instruction & practice

The families' role...

- ask your child to show you what he or she has learned
- look for ways to apply the learning in real-life situations

Our shared role...

- highlight and build on the students' strengths
- celebrate questions, mistakes, growth, effort, and struggle

Additional Resources

GRADE 3 FAMILY AND COMMUNITY RESOURCES OVERVIEW

RELATED ARTS MATHEMATICS LANGUAGE ARTS SCIENCE SOCIAL STUDIES HEALTH

The Howard County Public Schools (HCPSS) is nationally recognized for its rigorous learning. Our rigorous curriculum is designed to provide students a thorough grounding in essential knowledge and skills that will give them a leading edge in tomorrow's global environment. Our curriculum challenges students to think strategically, solve problems, innovate, collaborate, communicate effectively, and achieve goals.

Overview

What Your Child Will Learn

How to Support Your Child

Additional Resources



The HCPSS curriculum is aligned to the Common Core State Standards. These standards for literacy and mathematics education resulted from a state-led effort coordinated by the National Governors Association Center for Best Practices (NGA Center) and the Council of Chief State School Officers (CCSSO). The Standards were developed in collaboration with teachers, school administrators, and experts, to provide a clear and consistent framework to prepare our children for college and the workforce. [Additional information about the Common Core State Standards](#) .

HCPSS Curriculum is:

- 1. Deep:** Mastery of essential skills is emphasized at each level, so students build the skills and confidence to tackle more advanced concepts.
- 2. Broad:** Instruction crosses content areas – for example, science and social studies curriculum incorporates reading, math, and writing skills
- 3. Relevant:** Classroom lessons are reinforced through hands-on activities and real-world experiences.

Additional Resources

GRADE 4 FAMILY AND COMMUNITY RESOURCES MATHEMATICS • HOW TO SUPPORT YOUR CHILD

RELATED ARTS

MATHEMATICS

LANGUAGE ARTS

SCIENCE

SOCIAL STUDIES

HEALTH

How to Support Your Child Resources



[Whole Numbers](#)



[Multiplication and Division](#)



[Fractions](#)



[Decimals](#)



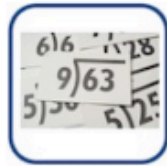
[Measurement and Data](#)



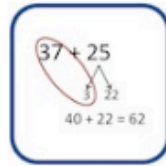
[Geometry](#)



[Patterns](#)



[Basic Facts](#)



[Computational Fluency](#)



[iTunes Mobile Apps](#)



[Android Mobile Apps](#)

Additional Resources

Multiplication and Division Online Activities

Multiplication and Division



[Thinking Blocks- Multiplication and Division](#) [↗]



[Quotient Cafe](#) [↗]



[Study Jams Divisibility Rules](#) [↗]



[The Product Game](#) [↗]



[Remainders Count](#) [↗]



[Demolition Division](#) [↗]

Factoring



[Factorize](#) [↗]



[Factor Game](#) [↗]



[Beematics](#) [↗]



[The Factor Tree Game](#) [↗]



[Not A Factor](#) [↗]



[Study Jams Multiples](#) [↗]



[Factor Trees](#) [↗]

Word Problems



[Thinking Blocks- Multiplication and Division Word Problems](#) [↗]



[Grand Slam Math](#) [↗]



[Multistep Word Problems](#) [↗]



[Hoops](#) [↗]